

# Quiz

## Student Name:

Each question is worth two points. You must show all your work to receive full credit.

1. Evaluate the following expression. Round your answer to the nearest tenth.

$$\begin{aligned}
 &40(1+0.02)^{23-10} \\
 &40(1.02)^{23-10} \\
 &40(1.02)^{13} && \mathbf{51.7} \\
 &40(1.29)
 \end{aligned}$$

2. Algebraically solve the following equation for  $x$ . Round your answer to the nearest tenth.

$$\begin{aligned}
 &52=13(2.05)^x \\
 &\left(\frac{52}{13}\right)=2.05^x && \mathbf{1.9} \\
 &x=\log_{2.05}\left(\frac{52}{13}\right)
 \end{aligned}$$

The following three questions are all based on Capital City, USA. The population of Capital City in 2000 was 3,271. The city was growing at a rate of 1.19%.

3. Write an exponential function that models population  $P$  as a function of year  $t$ .

$$P(t)=3271(1+0.0119)^{t-2000}$$

4. Use this model to predict the population of Capital City, USA in 2020.

$$\begin{aligned}
 &P(2020)=327(1+0.0119)^{2020-2000} \\
 &P(2020)=3271(1.0119)^{2020-2000} && \mathbf{4,154} \\
 &P(2020)=3271(1.0119)^{20} \\
 &P(2020)=3271(1.27)
 \end{aligned}$$

## TEACHING HUMAN DIGNITY

5. Use this model to estimate the year in which the population of Capital City, USA will reach 5,000.

$$5,000 = 3,271(1 + 0.0119)^{t-2000}$$

$$5,000 = 3,271(1.0119)^{t-2000}$$

$$\left(\frac{5,000}{3,271}\right) = (1.0119)^{t-2000}$$

During 2035

$$\log_{1.0119} \left(\frac{5,000}{3,271}\right) = t - 2000$$

$$t = 2000 + \log_{1.0119} \left(\frac{5,000}{3,271}\right)$$

$$t = 2035.9$$

6. Explain how you arrived at your answer to #5. (This explanation can include an explanation of your computation as well as any rounding that may have happened.)

**A strict calculation will yeild 2035.9. This means that the population will reach 5,000 during the year 2035; you can not just round to the nearest whole number.**